# Distributed V-Formation with Dynamic Neighborhood Resizing

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## Problem

**Hypothesis**: Bird flocking can be modeled as a Markov decision process

V-formation preserves energy

How to reach and maintain a V-formation for an arbitrary flock of *B* birds in distributed way?

#### Model

**States** (positions, velocities):  $s(t) = \{x_i(t), v_i(t)\}_{i=1}^B$ 

**Transitions:** 

$$x_i(t+1) = x_i(t) + v_i(t+1) + \xi,$$
  
 $v_i(t+1) = v_i(t) + a_i(t) + \nu,$ 

 $a_i(t)$  – controlled accelerations,  $\xi, \nu$  – noises

**Costs:**  $\sum$  of squared distances from the optimal

- clear view
  velocity matching
  upwash benefit
- 2 0 1 2 0 2 0 2 4 6 7 7

$$J(s_{a^h}(t+h)) \rightarrow \min_{a^h(t)}$$

s.t.  $||v_i(t)|| \leqslant v_{max}, ||a_i^h(t)|| \leqslant \rho ||v_i(t)|| \ \forall \ i = \overline{1,B}$ 

h – look-ahead

# Challenges

- Environmental uncertainties
- Nonlinear cost function
- Enormous state-space
- Real variables

## **Solution Approaches**

- Rule-based limited applicability
- Model-Predictive Control no guarantees

#### **Our Approach**

Input: an MDP in an arbitrary initial state

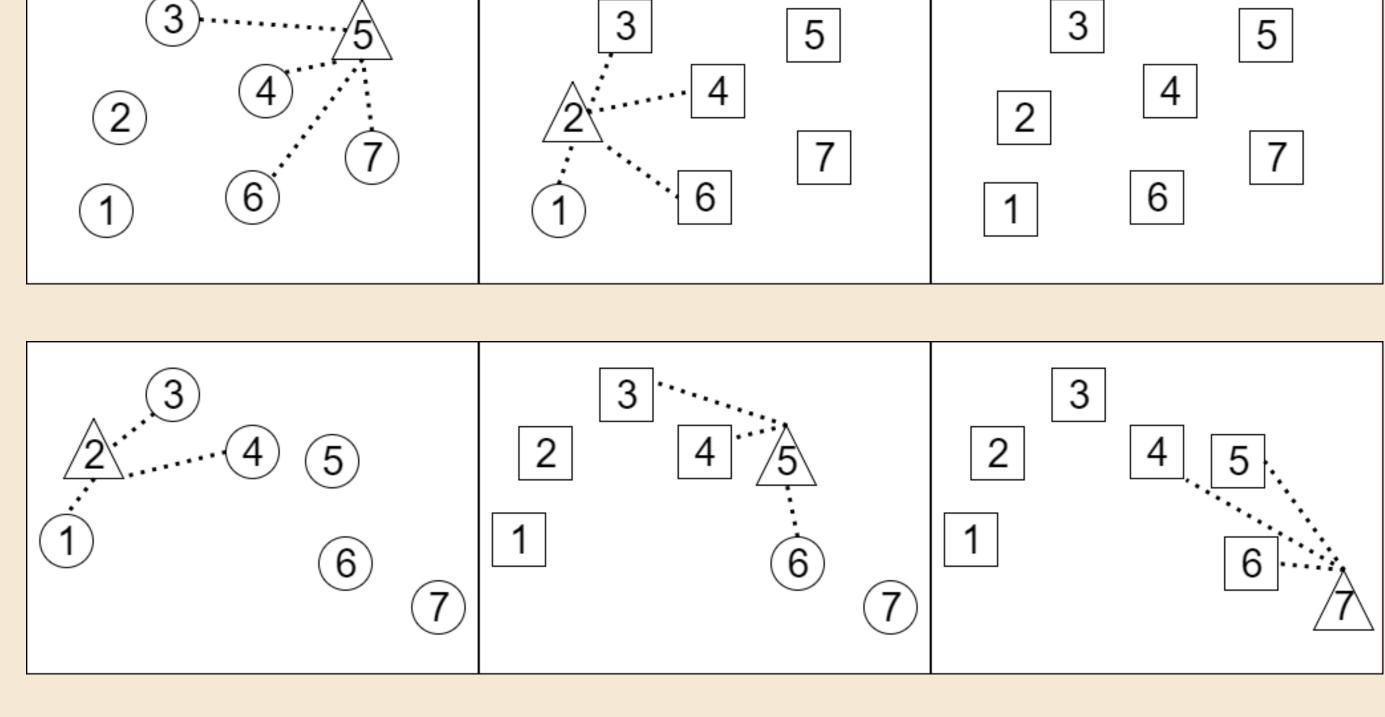
Output: distributed optimal control

Distributed Adaptive Horizon Adaptive Neighborhood Model Predictive Controller combines:

- Adaptive level-based horizon ⇒ convergence

#### **Distributed Control with Local Information and Consensus**

## **Adaptive neighborhood**



NeighSize $(J,J',k) = \min(\max(\lceil log_2(J) \rceil,0) + k_{min},k_{max})$ 

#### Adaptive horizon

